

A Level Maths Revision Checklist

Physics and Maths Tutor has loads of great resources to help to to revise:

Website	https://physicsandmathstutor.com
Edexcel	https://www.physicsandmathstutor.com/maths-revision/gcse-questi ons-edexcel/
OCR	https://www.physicsandmathstutor.com/maths-revision/gcse-questi ons-ocr/
AQA	<u>https://www.physicsandmathstutor.com/maths-revision/gcse-question/gcse-questi</u>

Pure

Pure	
Торіс	Objective
	Proof by deduction
	Proof by exhaustion
Proof	Disproof by counter example
	Proof by contradiction (including proof of the irrationality of 2 and the infinity of primes, and application to unfamiliar proofs).
	Understand and use the laws of indices for all rational exponents.
	Use and manipulate surds, including rationalising the denominator.
	Work with quadratic functions and their graphs.
	The discriminant of a quadratic function, including the conditions for real and repeated roots.
	Completing the square.
	Solution of quadratic equations, including solving quadratic equations in a function of the unknown.
	Solve simultaneous equations in two variables by elimination and by substitution, including one linear and one quadratic equation.
	Solve linear and quadratic inequalities in a single variable and interpret such inequalities graphically, including inequalities with brackets and fractions.
	Express solutions through correct use of 'and' and 'or', or through set notation.
	Represent linear and quadratic inequalities graphically.
	Manipulate polynomials algebraically, including expanding brackets and collecting like terms, factorisation and simple algebraic division; use of the factor theorem.
Algebra and functions	Simplify rational expressions, including by factorising and cancelling, and algebraic division (by linear expressions only).
	Understand and use graphs of functions; sketch curves defined by simple equations including polynomials
	The modulus of a linear function.
	Reciprocal functions (including their vertical and horizontal asymptotes)
	Interpret algebraic solution of equations graphically; use intersection points of graphs to solve equations.
	Understand and use proportional relationships and their graphs.
	Understand and use composite functions; inverse functions and their graphs.
	Understand the effect of simple transformations on the graph of $y = f(x)$, including sketching associated graphs: $y = af(x)$, $y = f(x) + a$, $y = f(x + a)$, $y = f(ax)$ and combinations of these transformations
	Decompose rational functions into partial fractions (denominators not more complicated than squared linear terms and with no more than 3 terms, numerators constant or linear).
	Use of functions in modelling, including consideration of limitations and refinements of the models.
	Understand and use the equation of a straight line.
	Gradient conditions for two straight lines to be parallel or perpendicular.
	Be able to use straight line models in a variety of contexts.
	Understand and use the coordinate geometry of the circle including using the equation of a circle in the form $(x - a)^2 + (y - b)^2 = r^2$
Coordinate geometry in the (x,y) plane	Completing the square to find the centre and radius of a circle; use of the following properties: • the angle in a semicircle is a right angle • the perpendicular from the centre to a chord bisects the chord • the radius of a circle at a given point on its circumference is perpendicular to
	the tangent to the circle at that point.
	Understand and use the parametric equations of curves and conversion between Cartesian and parametric forms
	Use parametric equations in modelling in a variety of contexts.

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	Independent and the bigenial comparison for second states of the second	
	Understand and use the binomial expansion for positive integer n; how other notations link to binomial probabilities.	
	Extend to any rational n, including its use for approximation; be aware that the expansion is valid for $\left \frac{bx}{a}\right < 1$ (proof not required)	
	Work with sequences including those given by a formula for the nth term and those generated by a simple relation of the form $x_{n+1}=f(x_n)$	
Sequences and series	increasing sequences; decreasing sequences; periodic sequences.	
	Understand and use sigma notation for sums of series.	
	Understand and work with arithmetic sequences and series, including the formulae for nth term and the sum to n terms	
	Understand and work with geometric sequences and series, including the formulae for the nth term and the sum of a finite geometric series; the sum to infinity of a convergent geometric series, including the use of $ r < 1$; modulus notation	
	Use sequences and series in modelling.	
	Understand and use the definitions of sine, cosine and tangent for all arguments;	
	the sine and cosine rules;	
	the area of a triangle	
	Work with radian measure, including use for arc length and area of sector.	\Box \Box
	Understand and use the standard small angle approximations of sine, cosine and tangent sin $\theta \approx \theta$, cos $\theta \approx 1 - \theta^2 / 2$, tan $\theta \approx \theta$ Where θ is in radians	
	Understand and use the sine, cosine and tangent functions; their graphs, symmetries and periodicity.	
Trigonometry	Know and use exact values of sin, cos and tan	
ingonometry	Understand and use the definitions of secant, cosecant and cotangent and of arcsin, arccos and arctan; their relationships to sine, cosine and tangent; understanding of their graphs; their ranges and domains.	
	Trigonometric identities	
	Double angle formulae and geometrical proofs of these formulae.	
	a sin(theta) + b cos(theta) = R cos(theta +/- alpha) or R sin(theta +/- alpha)	
	Construct proofs involving trigonometric functions and identities.	
	Use trigonometric functions to solve problems in context, including problems involving vectors, kinematics and forces.	
	Know and use the function a^x and its graph, where a is positive.	
	Know and use the function e^x and its graph	ΠΠ
	Know that the gradient of ekx is equal to kekx and hence understand why the exponential model is suitable in many applications.	
	Know and use the definition of loga x as the inverse of a x , where a is positive and x \Box 0. Know and use the function ln x and its graph. a \neq 1 Know and use ln x as the inverse function of ex	
	Understand and use the laws of logarithms: loga $x + \log a y = \log a (xy) \log a x$ - loga $y = \log a \square \square \square \square \square \square y x k \log a x = \log a xk$ (including, for example, $k = -1$ and $k = -12$)	
	Solve equations of the form a $x = b$	
Europeanticle and	Use logarithmic graphs to estimate parameters in relationships of the form $y =$	
Exponentials and logarithms	axn and $y = kbx$, given data for x and y	
logantining	Understand and use exponential growth and decay; use in modelling (examples may include the use of e in continuous compound interest, radioactive decay, drug concentration decay, exponential growth as a model for population growth); consideration of limitations and refinements of exponential models.	
	Understand and use the derivative of $f(x)$ as the gradient of the tangent to the graph of $y = f(x)$ at a general point (x, y) ; the gradient of the tangent as a limit; interpretation as a rate of change	
	sketching the gradient function for a given curve	
	second derivatives	
	differentiation from first principles for small positive integer powers of x and for sin x and cos x	

	Understand and use the second derivative as the rate of change of gradient;
	connection to convex and concave sections of curves and points of inflection. Differentiate xn , for rational values of n, and related constant multiples, sums and differences.
	Differentiate ekx and akx, sin kx, cos kx, tan kx and related sums, differences and constant multiples.
	Understand and use the derivative of In x
	Apply differentiation to find gradients, tangents and normals, maxima and minima and stationary points.
	points of inflection
	Identify where functions are increasing or decreasing. Differentiate using the product rule, the quotient rule and the chain rule, including problems involving connected rates of change and inverse functions.
	Differentiate simple functions and relations defined implicitly or parametrically, for first derivative only.
	Construct simple differential equations in pure mathematics and in context, (contexts may include kinematics, population growth and modelling the relationship between price and demand).
Differentiation	Know and use the Fundamental Theorem of Calculus
	Integrate xn (excluding n = -1) and related sums, differences and constant multiples
	Integrate ekx, 1 x , sinkx , cos kx and related sums, differences and constant multiples.
	Evaluate definite integrals; use a definite integral to find the area under a curve and the area between two curves
	Understand and use integration as the limit of a sum.
	Carry out simple cases of integration by substitution and integration by parts; understand these methods as the inverse processes of the chain and product rules respectively (Integration by substitution includes finding a suitable substitution and is limited to cases where one substitution will lead to a function which can be integrated; integration by parts includes more than one application of the method but excludes reduction formulae.)
	Integrate using partial fractions that are linear in the denominator.
	Evaluate the analytical solution of simple first order differential equations with separable variables, including finding particular solutions (Separation of variables may require factorisation involving a common factor.)
	Interpret the solution of a differential equation in the context of solving a problem, including identifying limitations of the solution; includes links to kinematics.
	Locate roots of $f(x) = 0$ by considering changes of sign of $f(x)$ in an interval of x on which $f(x)$ is sufficiently well behaved.
	Locate roots of $f(x) = 0$ by considering changes of sign of $f(x)$ in an interval of x on which $f(x)$ is sufficiently well behaved.
Numerical methods	Solve equations approximately using simple iterative methods; be able to draw associated cobweb and staircase diagrams.
	Solve equations using the Newton-Raphson method and other recurrence relations of the form $xn+1=g(xn)$ Understand how such methods can fail.
	Understand and use numerical integration of functions, including the use of the trapezium rule and estimating the approximate area under a curve and limits that it must lie between.
	Use numerical methods to solve problems in context.
	Use vectors in two dimensions and in three dimensions
	Calculate the magnitude and direction of a vector and convert between component form and magnitude/direction form.
Vectors	Add vectors diagrammatically and perform the algebraic operations of vector addition and multiplication by scalars, and understand their geometrical interpretations.
	Understand and use position vectors; calculate the distance between two points represented by position vectors.
	Use vectors to solve problems in pure mathematics and in context (including

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Statistics

Торіс	Objectives
	Understand and use the terms 'population' and 'sample'.
	Use samples to make informal inferences about the population.
Statistical sampling	Understand and use sampling techniques, including simple random sampling and opportunity sampling.
	Select or critique sampling techniques in the context of solving a statistical problem, including understanding that different samples can lead to different conclusions about the population.
	Interpret diagrams for single-variable data, including understanding that area in a histogram represents frequency.
	Connect to probability distributions.
	Interpret scatter diagrams and regression lines for bivariate data, including recognition of scatter diagrams which include distinct sections of the population (calculations involving regression lines are excluded).
	Understand informal interpretation of correlation.
Data presentation and interpretation	Understand that correlation does not imply causation.
and interpretation	Interpret measures of central tendency and variation, extending to standard deviation.
	Be able to calculate standard deviation, including from summary statistics.
	Recognise and interpret possible outliers in data sets and statistical diagrams.
	Select or critique data presentation techniques in the context of a statistical problem.
	Be able to clean data, including dealing with missing data, errors and outliers.
	Understand and use mutually exclusive and independent events when calculating probabilities.
	Link to discrete and continuous distributions.
Probability	Understand and use conditional probability, including the use of tree diagrams, Venn diagrams, two-way tables.
	Understand and use the conditional probability formula $P(A B) = P() P()$
	Modelling with probability, including critiquing assumptions made and the likely effect of more realistic assumptions.
	Understand and use simple, discrete probability distributions (calculation of mean and variance of discrete random variables is excluded), including the binomial distribution, as a model; calculate probabilities using the binomial distribution.
Statistical distributions	Understand and use the Normal distribution as a model; find probabilities using the Normal distribution
distributions	Link to histograms, mean, standard deviation, points of inflection and the binomial distribution
	Select an appropriate probability distribution for a context, with appropriate reasoning, including recognising when the binomial or Normal model may not be appropriate.
	Understand and apply the language of statistical hypothesis testing, developed through a binomial model: null hypothesis, alternative hypothesis, significance level, test statistic, 1-tail test, 2-tail test, critical value, critical region, acceptance region, p-value;
	extend to correlation coefficients as measures of how close data points lie to a straight line.
	be able to interpret a given correlation coefficient using a given p-value or critical value (calculation of correlation coefficients is excluded).
Hypothesis testing	Conduct a statistical hypothesis test for the proportion in the binomial distribution and interpret the results in context.
	Understand that a sample is being used to make an inference about the population
	appreciate that the significance level is the probability of incorrectly rejecting the null hypothesis.
	Conduct a statistical hypothesis test for the mean of a Normal distribution with known, given or assumed variance and interpret the results in context.

Mechanics

Торіс	Objectives	
Quantities and units in mechanics	Understand and use fundamental quantities and units in the S.I. system: length, time, mass.	
	Understand and use derived quantities and units: velocity, acceleration, force, weight, moment.	
	Understand and use the language of kinematics: position; displacement; distance travelled; velocity; speed; acceleration.	
	Understand, use and interpret graphs in kinematics for motion in a straight line: displacement against time and interpretation of gradient; velocity against time and interpretation of gradient and area under the graph.	
Kinematics	Understand, use and derive the formulae for constant acceleration for motion in a straight line.	
	Extend to 2 dimensions using vectors.	
	Use calculus in kinematics for motion in a straight line: SUVAT	
	Extend to 2 dimensions using vectors.	
	Model motion under gravity in a vertical plane using vectors; projectiles.	
	Understand the concept of a force; understand and use Newton's first law.	
Forces and Newton's laws	Understand and use Newton's second law for motion in a straight line (restricted to forces in two perpendicular directions or simple cases of forces given as 2-D vectors); extend to situations where forces need to be resolved (restricted to 2 dimensions).	
	Understand and use weight and motion in a straight line under gravity; gravitational acceleration, g, and its value in S.I. units to varying degrees of accuracy.	
	(The inverse square law for gravitation is not required and g may be assumed to be constant, but students should be aware that g is not a universal constant but depends on location.)	
	Understand and use Newton's third law; equilibrium of forces on a particle and motion in a straight line (restricted to forces in two perpendicular directions or simple cases of forces given as 2-D vectors); application to problems involving smooth pulleys and connected particles; resolving forces in 2 dimensions; equilibrium of a particle under coplanar forces.	
	Understand and use addition of forces; resultant forces; dynamics for motion in a plane.	
	Understand and use the F $\leq \mu$ R model for friction; coefficient of friction; motion of a body on a rough surface; limiting friction and statics.	
Moments	Understand and use moments in simple static contexts.	

Revision Tips

The exercises in your textbook are designed to "scaffold" your learning. It's teacher-talk for supporting you to understand harder topics. Once you understand them you don't need the scaffolding any more.

If you're struggling with exam questions consider going back to the textbook exercises and think about what each one is trying to help you to understand.

Don't forget to refer to the objectives in your checklist. Which ones apply to that exam question? It will help you to understand where your problem is.

Try exam questions in stages.

1. Can you do it without notes?

2. Can you do it with the textbook or YouTube to help?

3. Do you follow the solution when a friend or teacher explains it?

4. If you're really stuck get the markscheme out. You could try covering it with a piece of paper so that you can only see one mark at a time. Perhaps if you know how to start you can get further?

Think of your learning in two compartments - there are the techniques which textbook exercises practice, and then the skill of applying those techniques to an exam question.

Skill is being able to choose and apply techniques. The techniques are the repetitive bit - you want to be fast and accurate when performing them.

Skill is always harder to develop, because you need to have mastered the techniques!